

Specific Performance Criteria	Intermediate Learning Objectives
<p>1. <i>Functions</i></p> <p>1.1 Recognition of functions</p> <p>1.2 Finding domain, range and intercepts</p> <p>1.3 Graphing of functions</p> <p>1.4 Operations on functions</p> <p>1.5 Appropriate use of functions to represent given situations</p>	<p>1.1.1. Decide whether a given relation is a function from its graphical representation.</p> <p>1.1.2. Recognize and name the following functions from their symbolic representations:</p> <p>$f(x) = c$ constant function</p> <p>$f(x) = ax + b$ linear function</p> <p>$f(x) = ax^2 + bx + c$ quadratic function</p> <p>$f(x) = x$ absolute value function</p> <p>$f(x) = \sqrt{x}$ square root function</p> <p>$f(x) = a^x$ exponential function</p> <p>$f(x) = \log_a x$ logarithmic function</p> <p>$f(x) = \sin x$ sine function</p> <p>$f(x) = \cos x$ cosine function</p> <p>$f(x) = \tan x$ tangent function</p> <p>$f(x) = \csc x$ cosecant function</p> <p>$f(x) = \sec x$ secant function</p> <p>$f(x) = \cot x$ cotangent function</p> <p>1.1.3. Recognize and name the following function from its symbolic representation: $f(x) = \sqrt[n]{x}$ (nth root function).</p> <p>1.1.4. Recognize and name the functions listed in 1.1.2 from their graphical representations.</p> <p>1.2.1. Find and state the domain of functions listed in 1.1.2 from both their graphical and their symbolic representations.</p> <p>1.2.2. Find and state the range of functions listed in 1.1.2 and 1.1.3 from both their graphical and their symbolic representations.</p> <p>1.2.3. Find and state the x- and y-intercepts, if they exist, of functions listed in 1.1.2 from both their graphical and their symbolic representations.</p> <p>1.3.1. Graph the functions listed in 1.1.2.</p> <p>1.3.2. Graph piecewise defined functions whose pieces are made up of the functions listed in 1.1.2.</p> <p>1.3.3. Apply vertical and horizontal shifts and reflections about the horizontal and vertical axes, and any combination of these to the functions listed in 1.1.2.</p> <p>1.4.1. Perform addition, subtraction, multiplication, division and composition of functions.</p> <p>1.4.2. Divide two polynomial functions and express the answer in the form</p> $\frac{p(x)}{d(x)} = q(x) + \frac{r(x)}{d(x)}.$ <p>1.4.3. Find the value of a function at a point in its domain.</p> <p>1.4.4. Evaluate $\frac{f(x+h) - f(x)}{h}$ (the difference quotient) for linear, quadratic and simple rational functions.</p> <p>1.5.1. Given an applied problem, decide which function best represents the situation and express the relationship using appropriate notation.</p>
<p>2. <i>Limits, Continuity and Derivatives</i></p> <p>2.1 Determination of Limits</p> <p>2.2 Determination of whether a function is continuous at a point or on an interval</p>	<p>2.1.1. Give an intuitive description of the limit of a function at a point.</p> <p>2.1.2. Evaluate a limit of a function by viewing the graph of the function.</p> <p>2.1.3. Estimate a limit numerically by using successive approximations (using a table of values).</p> <p>2.1.4. Evaluate a limit analytically by direct substitution, factoring, rationalizing or simplifying rational expressions.</p> <p>2.1.5. Evaluate analytically limits at infinity.</p> <p>2.1.6. Evaluate one-sided limits.</p> <p>2.1.7. Recognize and evaluate infinite limits.</p> <p>2.2.1. Define continuity of a function at a point; that is, state the three conditions which must be satisfied in order that a function be continuous at a point.</p> <p>2.2.2. Use the definition of continuity to determine if a function is continuous at a specific point.</p> <p>2.2.3. Determine on which interval(s) a function is continuous.</p>

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<p>2.3 Use of the limit definition of the derivative</p> <p>2.4 Use of the graph of a function to determine whether a function is differentiable at a point or on an interval</p>	<p>2.3.1. Define the derivative of a function as (i) the limit of a difference quotient, (ii) the slope of a tangent line, and (iii) the rate of change (in particular the velocity function associated with a position function).</p> <p>2.3.2. Use the limit definition of the derivative to determine the derivative of a polynomial of degree 1, 2 or 3, square root and simple rational functions.</p> <p>2.3.3. Use the limit definition of the derivative to determine the numerical value of the derivative at a given point.</p> <p>2.3.4. Use the limit definition of the derivative to determine the slope of the tangent line to a curve at a specific point.</p> <p>2.3.5. Use the limit definition of the derivative to determine the equation of the tangent line to a curve at a specific point.</p> <p>2.4.1. Determine if the derivative of a function exists at a point or on an interval by examining the graph of the function.</p>
<p>3. <i>Rules and Techniques of Differentiation</i></p>	
<p>3.1 Recognition of the equivalence of various derivative notations</p>	<p>3.1.1. Recognize different notations for the derivative of y with respect to x:</p> $y', f'(x), \frac{dy}{dx}, \frac{d}{dx}f(x), D_x y$
<p>3.2 Use of basic differentiation formulas and rules and proof of simple propositions</p>	<p>3.2.1. Recognize when and how to use the basic differentiation formulas:</p> $\begin{array}{ll} \frac{d}{dx}[c] = 0 & \frac{d}{dx}[\sin x] = \cos x \\ \frac{d}{dx}[x^n] = nx^{n-1} & \frac{d}{dx}[\cos x] = -\sin x \\ \frac{d}{dx}[e^x] = e^x & \frac{d}{dx}[\tan x] = \sec^2 x \\ \frac{d}{dx}[\ln x] = \frac{1}{x} & \frac{d}{dx}[\sec x] = \sec x \tan x \\ \frac{d}{dx}[a^x] = a^x \ln a & \frac{d}{dx}[\csc x] = -\csc x \cot x \\ \frac{d}{dx}[\log_a x] = \frac{1}{x \ln a} & \frac{d}{dx}[\cot x] = -\csc^2 x \end{array}$ <p>3.2.2. Recognize when and how to use the following differentiation formulas derived from the chain rule:</p> $\begin{array}{ll} \frac{d}{dx}[u^n] = nu^{n-1}u' & \frac{d}{dx}[\sin u] = \cos u u' \\ \frac{d}{dx}[e^u] = e^u u' & \frac{d}{dx}[\cos u] = -\sin u u' \\ \frac{d}{dx}[\ln u] = \frac{u'}{u} & \frac{d}{dx}[\tan u] = \sec^2 u u' \\ \frac{d}{dx}[a^u] = a^u (\ln a) u' & \frac{d}{dx}[\sec u] = \sec u \tan u u' \\ \frac{d}{dx}[\log_a u] = \frac{u'}{u \ln a} & \frac{d}{dx}[\csc u] = -\csc u \cot u u' \\ & \frac{d}{dx}[\cot u] = -\csc^2 u u' \end{array}$ <p>3.2.3. Recognize when and how to use the following rules: constant rule, power rule, constant multiple rule, sum and difference rule.</p> <p>3.2.4. Recognize when and how to use the product, quotient and chain rules.</p> <p>3.2.5. Prove a selection of the rules in 3.2.1 using the limit definition of the derivative.</p>
<p>3.3 Determination of whether a function is differentiable at a point or on an interval</p>	<p>3.3.1. Determine whether a function is differentiable at a specified point or on an interval using graphical, numerical, or analytical methods.</p>
<p>3.4 Use of differentiation rules to perform implicit and logarithmic differentiation</p>	<p>3.4.1. Recognize when and how to use implicit differentiation.</p> <p>3.4.2. Recognize when and how to use logarithmic differentiation.</p>
<p>3.5 Evaluation and application of higher order derivatives</p>	<p>3.5.1. Find higher order derivatives.</p> <p>3.5.2. Use higher-order derivatives to solve position, velocity and acceleration problems.</p>
<p>3.6 Use of derivatives to find the slope of a tangent (normal) line to a curve at a point</p>	<p>3.6.1. Use the differentiation rules listed in 3.2.1 and 3.2.2 to find the slope of the tangent line to a curve at a point.</p> <p>3.6.2. Use the differentiation rules listed in 3.2.1 and 3.2.2 to find the equation of the tangent line to a curve at a point.</p> <p>3.6.3. Use the differentiation rules listed in 3.2.1 and 3.2.2 to find the equation of the normal line to a curve at a point.</p>

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<p>4. <i>Graphing of Functions</i></p> <p>4.1 Use of the derivative and related concepts to analyze the variations of a function and to sketch a graph of the function</p> <p>4.2 Demonstration of the ability to understand abstract properties of continuous and differentiable functions, as illustrated by two simple standard theorems.</p>	<p>4.1.1. Find critical numbers.</p> <p>4.1.2. Find intervals on which a function is increasing and decreasing using the sign of the first derivative.</p> <p>4.1.3. Find relative and absolute extrema.</p> <p>4.1.4. Use the first or second derivative test to decide whether the critical points represent relative maxima or relative minima.</p> <p>4.1.5. Find inflection points.</p> <p>4.1.6. Find intervals on which a function is concave up or concave down using the sign of the second derivative.</p> <p>4.1.7. Use limits to find all vertical and horizontal asymptotes.</p> <p>4.1.8. Use 4.1.1–4.1.7 to graph polynomial, rational, trigonometric, logarithmic and exponential functions.</p> <p>4.2.1. State the conditions necessary for Rolle’s Theorem.</p> <p>4.2.2. State the conclusion of Rolle’s Theorem.</p> <p>4.2.3. State the conditions necessary for the Mean Value Theorem.</p> <p>4.2.4. State the conclusion of the Mean Value Theorem.</p>
<p>5. <i>Optimization and Rate-of-Change Problems</i></p> <p>5.1 Solution of optimization problems</p> <p>5.2 Solution of problems involving related rates</p>	<p>5.1.1. Represent an optimization word problem in functional form.</p> <p>5.1.2. Determine the quantity, P, to be maximized or minimized and identify the variables which are involved.</p> <p>5.1.3. Draw a diagram, if possible, to illustrate the problem and list any other relationship(s) between the variables.</p> <p>5.1.4. Express P as a function of one variable.</p> <p>5.1.5. Find the derivative of the function for P obtained in 5.1.4.</p> <p>5.1.6. Find all the possible critical values by solving the equation $P' = 0$.</p> <p>5.1.7. Test the critical value(s) and interval endpoints for absolute maximum or minimum.</p> <p>5.1.8. Interpret (explain) the results found in the optimization problem.</p> <p>5.2.1. Represent a word problem involving related rates in functional form.</p> <p>5.2.2. Identify the variables and rates in the problem.</p> <p>5.2.3. Draw a diagram, if possible, to illustrate the problem.</p> <p>5.2.4. Determine the equation relating the variables.</p> <p>5.2.5. Differentiate the equation in 5.2.4 with respect to time, t.</p> <p>5.2.6. Solve the equation in 5.2.5 for the required rate.</p> <p>5.2.7. Interpret (explain) the results found in the problem involving related rates.</p>
<p>6. <i>Integration</i></p> <p>6.1 Evaluation of the indefinite integral</p> <p>6.2 Evaluation of the definite integral</p> <p>6.3 Solution of simple differential equations</p>	<p>6.1.1. Give the definition of the indefinite integral as an antiderivative.</p> <p>6.1.2. Express the basic differentiation formulas listed in 3.2.1 as antidifferentiation formulas.</p> <p>6.1.3. Recognize when and how to use the constant multiple rule and the sum and difference rule in the evaluation of integrals.</p> <p>6.1.4. Use the antidifferentiation formulas from 6.1.2 and the rules in 6.1.3 to evaluate indefinite integrals.</p> <p>6.2.1. State the definition of the definite integral.</p> <p>6.2.2. State the Fundamental Theorem of Calculus.</p> <p>6.2.3. Find the definite integral of functions described in 6.1.</p> <p>6.2.4. Use the Fundamental Theorem of Calculus to find the area of a region under a curve on a closed interval.</p> <p>6.3.1. Find the general solution to a differential equation of the form $y' = f(x)$.</p> <p>6.3.2. Find the particular solution to a differential equation of the form $y' = f(x)$ given an initial condition $y(a) = b$.</p>

Teaching Methods. This course will be 75 hours, meeting three times a week for a total of five hours a week. It relies mainly on the lecture method, although some of the following techniques are also used: question-and-answer sessions, labs, problem solving periods, class discussions, and assigned reading for independent study. In general, each class begins with a question period on previous topics, then new material is introduced, followed by worked examples. No marks are deducted for absenteeism (however, see below). Failure to keep pace with the lectures results in a cumulative inability to cope with the material and a failure in the course. A student will generally succeed or fail depending on how many problems have been attempted and solved successfully. It is entirely the student’s responsibility to complete suggested homework assignments as soon as possible following the lecture, as the material will be fresher in his/her mind. This also allows the student the maximum benefit from any discussion of the homework (which usually occurs in the following class). Answers to a selected number of problems can be found in the back of the text. Individual teachers may provide supplementary notes and problems as they see fit.

Course Content (with selected exercises). This is a *minimal* list of exercises which you should attempt, assuming you are also doing regular homework (e.g., WEBWORK) assigned by your instructor.

1.1: 1, 2, 7, 9, 14, 49, 55, 63, 72, 73

1.2: 1, 3, 8, 10, 11, 17

1.3: 3, 6, 12, 24, 30, 31, 37, 41, 45, 53, 61, 63, 65

1.4: 12, 14, 21, 23, 30, 37

1.5: 18, 21, 37, 41, 50, 53, 56, 61

Chap. 1 Review (p. 69): 2, 10, 17, 18, 23, 24, 25a, 25b

2.1: [instructor's discretion]

2.2: 6, 9, 11, 17, 31, 35, 40

2.3: 2, 9, 15, 19, 23, 29, 37, 40, 43, 45, 53, 59, 64, 65

2.4: [instructor's discretion]

2.5: 4, 7, 21, 33, 35, 41, 46, 47, 52, 69, 71

2.6: 4, 9, 21, 24, 29, 32, 33, 39, 45, 49, 52, 54, 59, 63, 67

2.7: 3, 8, 10, 11, 17, 22, 23, 28, 35, 37, 39, 59, 60

2.8: 3, 25, 28, 30, 43, 51, 57, 63, 67

Chap. 2 Review (p. 166): 1, 2, 8, 12, 15, 17, 20, 22, 23, 29, 33, 36, 43, 47, 54

3.1: 3, 9, 23, 24, 27, 31, 37, 55, 60, 62, 66, 69, 81, 83, 86

3.2: 9, 15, 20, 23, 25, 26, 27, 32, 41, 44, 48, 49, 52, 53, 62

3.3: 5, 8, 13, 16, 20, 22, 32, 34, 37, 43, 45, 50, 52, 54, 58

3.4: 19, 25, 38, 40, 41, 44, 45, 48, 53, 59, 65, 74, 76, 78, 84

3.5: 7, 16, 19, 20, 21, 23, 29, 38, 39, 43, 46, 75, 77, 79, 80

3.6: 9, 12, 13, 21, 22, 29, 34, 40, 42, 45, 49, 50, 52, 56

3.7: 1, 5, 10

3.8: [instructor's discretion]

3.9: 12, 18, 23, 27, 29, 30, 33, 42, 44, 47, 50

Chap. 3 Review (p. 267): 28, 37, 41, 50, 53, 59, 60, 66, 81, 85, 89, 95, 98, 109, 112

4.1: 5, 7, 10, 13, 27, 39, 43, 44, 51, 56, 57, 63, 67, 72, 77

4.2: 9, 12, 18, 19, 22, 24, 25, 37, 38

4.3: 8, 11, 12, 16, 18, 19, 27, 30, 35, 45, 47, 55, 60, 75, 79, 82

4.5: 7, 13, 15, 24, 27, 30, 34, 39, 40, 43, 46, 50

4.7: 13, 16, 22, 33, 34, 36, 39, 50, 58, 68, 71, 73, 74

4.9: 5, 12, 15, 16, 29, 37, 38, 47, 50, 53, 55, 61, 63, 69, 77

Chap. 4 Review (p. 359): 5, 6, 17, 24, 29, 32, 47, 54, 72, 74, 78, 79, 84, 85

5.1: 5, 7, 17, 21, 25, 27

5.2: 4, 7, 17, 25, 30, 33, 37, 49, 53

5.3: 3, 7, 18, 26, 29, 33, 37, 41, 43, 63, 65, 73, 75, 83

5.4: 1, 4, 9, 14, 15, 16, 18, 29, 31, 37, 38, 46, 49, 61, 71

Chap. 5 Review (p. 422): 2, 5, 7, 12, 25, 40, 49, 58, 62, 67, 72

To strengthen your skills with more practice, attempt any of the exercises in the sections above which not omitted explicitly below. While doing so, it is a good idea to focus on types of problems with which you struggle.

Practice exercises: Omissions

1.5: Omit 63–76

Chap. 1 Review: omit 25c, 25d, 26d

2.5: omit 29, 32, 60

2.6: omit 35, 40

Chap. 2 Review: omit 19

3.5: omit 17, 49–64

Chap. 3 Review: omit 6, 12, 17, 31, 38, 43, 45, 47, 48

4.1: omit 42, 62

4.2: omit 34, 35

4.3: omit 56, 64

4.5: omit 41, 42, 45, 48, 51–54, 71

4.9: omit 18, 19, 22, 24, 33, 44

Chap. 4 Review: omit 7–14, 31, 33, 34, 61–64, 66, 68, 73, 81–83

5.3: omit 38, 39, 42, 62

5.4: omit 12, 13, 30, 40, 41, 43, 48

Chap. 5 Review: omit 8, 14, 17–24, 26–38, 41, 42, 44, 56, 63, 65, 66, 71

Other Resources.

Math Website.

<http://departments.johnabbott.qc.ca/departments/mathematics>

Math Study Area. Located in H-200A and H-200B; the common area is usually open from 8:30 to 17:30 on weekdays as a quiet study space. Computers and printers are available for math-related assignments. It is also possible to borrow course materials when the attendant is present.

Math Help Centre. Located near H-211; teachers are on duty from 9:00 until 16:00 to give math help on a drop-in basis.

Peer Tutoring. Starting on the fifth week of each semester, first year students can be paired with a fellow finishing student for a weekly appointment of tutoring. Ask your teacher for details.

Academic Success Centre. The Academic Success Centre, located in H-117, offers study skills workshops and individual tutoring.

Departmental Attendance Policy. Regular attendance is expected. Missing six classes is grounds for automatic failure in this course. Many of the failures in this course are due to students missing classes.

Evaluation Plan. A student's Final Grade is a combination of the Class Mark and the mark on the Final Exam. The Class Mark will be 75% (three to five tests) and 25% at your teacher's discretion (more tests, quizzes or assignments). The specifics of the Class Mark are included in an appendix that is distributed to students along with this course outline. The Final Exam is set by the NYA course committee (which consists of all instructors currently teaching this course), and is marked by each individual instructor. Every effort is made to ensure equivalence between the various sections of the course.

The Final Grade will be the better of:

50% Class Mark and 50% Final Exam Mark

or

25% Class Mark and 75% Final Exam Mark

A student *choosing not to write* the Final Exam will receive a failing grade of 50% or their Class Mark, whichever is less.

Students must be available until the end of the final examination period to write exams.

Course Costs. In addition to the cost of the textbook (see above), your instructor might recommend you acquire an inexpensive scientific calculator (\$15-\$25). *No calculators are allowed during tests or the final exam.*

College Policies. Article numbers refer to the IPESA (Institutional Policy on the Evaluation of Student Achievement, available at <http://johnabbott.qc.ca/ipesa>). Students are encouraged to consult the IPESA to learn more about their rights and responsibilities.

Changes to Evaluation Plan in Course Outline (Article 4.3). Changes to the evaluation plan, during the semester, require unanimous consent.

Mid-Semester Assessment MSA (Article 3.3). Students will receive an MSA in accordance with College procedures.

Religious Holidays (Article 3.2). Students who wish to observe religious holidays must inform their teacher in writing within the first two weeks of the semester of their intent.

Grade Reviews (Article 3.2, item 19). It is the responsibility of students to keep all assessed material returned to them in the event of a grade review. (The deadline for a Grade Review is 4 weeks after the start of the next regular semester.)

Results of Evaluations (Article 3.3, item 7). Students have the right to receive the results of evaluation, for regular day division courses, within two weeks. For evaluations at the end of the semester/course, the results must be given to the student by the grade submission deadline.

Cheating and Plagiarism (Articles 8.1 & 8.2). Cheating and plagiarism are serious infractions against academic integrity, which is highly valued at the College; they are unacceptable at John Abbott College. Students are expected to conduct themselves accordingly and must be responsible for all of their actions.